

# TREE RECURSION AND DATA ABSTRACTION

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COMPUTER SCIENCE MENTORS 61A

February 12, 2018 to February 14, 2018

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## Recursion

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1. Write a function `is_sorted` that takes in an integer `n` and returns true if the digits of that number are increasing from right to left.

```
def is_sorted(n):  
    """  
    >>> is_sorted(2)  
    True  
    >>> is_sorted(22222)  
    True  
    >>> is_sorted(9876543210)  
    True  
    >>> is_sorted(9087654321)  
    False  
    """
```

**Solution:**

```
right_digit = n % 10  
rest = n // 10  
if rest == 0:  
    return True  
elif right_digit > rest % 10:  
    return False  
else:  
    return is_sorted(rest)
```

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**Tree Recursion**

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1. Mario needs to jump over a series of Piranha plants, represented as a string of 0's and 1's. Mario only moves forward and can either *step* (move forward one space) or *jump* (move forward two spaces) from each position. How many different ways can Mario traverse a level without stepping or jumping into a Piranha plant? Assume that every level begins with a 1 (where Mario starts) and ends with a 1 (where Mario must end up).

```
def mario_number(level):
    """
    Return the number of ways that Mario can traverse the
    level, where Mario can either hop by one digit or two
    digits each turn. A level is defined as being an integer
    with digits where a 1 is something Mario can step on and 0
    is
    something Mario cannot step on.
    >>> mario_number(10101)
    1
    >>> mario_number(11101)
    2
    >>> mario_number(100101)
    0
    """
    if _____:
        _____
    elif _____:
        _____
    else:
        _____
```

**Solution:**

```
def mario_number(level):
    """
    Return the number of ways that mario can traverse the
    level where mario can either hop by one digit or two
    digits each turn a level is defined as being an integer
    where a 1 is something mario can step on and 0 is
    something mario cannot step on.
    >>> mario_number(10101)
    1
    >>> mario_number(11101)
    2
    >>> mario_number(100101)
    0
    """
    if level == 1:
        return 1
    elif level % 10 == 0:
        return 0
    else:
        return mario_number(level // 10) + mario_number((
            level // 10) // 10)
```

2. Implement the function `make_change`. You may not need to use all the lines.

```
def make_change(n):
    """Write a function, make_change that takes in an
    integer amount, n, and returns the minimum number
    of coins we can use to make change for that n,
    using 1-cent, 3-cent, and 4-cent coins.
    Look at the doctests for more examples.
    >>> make_change(5)
    2
    >>> make_change(6) # tricky! Not 4 + 1 + 1 but 3 + 3
    2
    """
    if _____:
        return 0
    elif _____:
        return _____
    elif _____:
        _____
        _____
        return _____
    else:
        _____
        _____
        return _____
```

**Solution:**

```
def make_change(n):
    """Write a function, make_change that takes in an
    integer amount, n, and returns the minimum number
    of coins we can use to make change for that n,
    using 1-cent, 3-cent, and 4-cent coins.
    Look at the doctests for more examples.
    >>> make_change(5)
    2
    >>> make_change(6) # tricky! Not 4 + 1 + 1 but 3 + 3
    2
    """
    if n < 1:
        return 0
    elif n < 3:
        return 1 + make_change(n - 1) # (return n) is also
        fine
    elif n < 4:
        use_1 = 1 + make_change(n - 1)
        use_3 = 1 + make_change(n - 3)
        return min(use_1, use_3)
    else:
        use_1 = 1 + make_change(n - 1)
        use_3 = 1 + make_change(n - 3)
        use_4 = 1 + make_change(n - 4)
        return min(use_1, use_3, use_4)
```

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**Data Abstraction**

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1. The following is an **Abstract Data Type (ADT)** for elephants. Each elephant keeps track of its name, age, and whether or not it can fly. Given our provided constructor, fill out the selectors:

```
def elephant(name, age, can_fly):  
    """  
    Takes in a string name, an int age, and a boolean can_fly.  
    Constructs an elephant with these attributes.  
    >>> dumbo = elephant("Dumbo", 10, True)  
    >>> elephant_name(dumbo)  
    "Dumbo"  
    >>> elephant_age(dumbo)  
    10  
    >>> elephant_can_fly(dumbo)  
    True  
    """  
    return [name, age, can_fly]  
def elephant_name(e):
```

**Solution:**

```
return e[0]
```

```
def elephant_age(e):
```

**Solution:**

```
return e[1]
```

```
def elephant_can_fly(e):
```

**Solution:**

```
return e[2]
```

2. This function returns the correct result, but there's something wrong about its implementation. How do we fix it?

```
def elephant_roster(elephants):  
    """  
    Takes in a list of elephants and returns a list of their  
    names.  
    """  
    return [elephant[0] for elephant in elephants]
```

**Solution:**

elephant[0] is a Data Abstraction Violation (DAV).  
We should use a selector instead.

3. Fill out the following constructor for the given selectors.

```
def elephant(name, age, can_fly):
```

**Solution:**

```
    return [[name, age], can_fly]
```

```
def elephant_name(e):  
    return e[0][0]  
def elephant_age(e):  
    return e[0][1]  
def elephant_can_fly(e):  
    return e[1]
```

4. How can we write the fixed `elephant_roster` function for the constructors and selectors in the previous question?

**Solution:** No change is necessary to fix `elephant_roster` since using the `elephant` selectors “protects” the roster from constructor definition changes.

5. (Optional) Fill out the following constructor for the given selectors.

```
def elephant(name, age, can_fly):  
    """  
    >>> chris = elephant("Chris Martin", 38, False)  
    >>> elephant_name(chris)  
        "Chris Martin"  
    >>> elephant_age(chris)  
        38  
    >>> elephant_can_fly(chris)  
        False  
    """  
    def select(command)
```

**Solution:**

```
        if command == "name":  
            return name  
        elif command == "age":  
            return age  
        elif command == "can_fly":  
            return can_fly  
        return "Breaking abstraction barrier!"  
    return select  
def elephant_name(e):  
    return e("name")  
def elephant_age(e):  
    return e("age")  
def elephant_can_fly(e):  
    return e("can_fly")
```