

MORE SCHEME

COMPUTER SCIENCE MENTORS 61A

April 2 to April 4, 2018

1 Scheme

1. What will Scheme output? Draw box-and-pointer diagrams to help determine this.

(a) `(cons (cons 1 nil) (cons 2 (cons (cons 3 (cons 4 5)) (cons 6 nil))))`

(b) `(cons (cons (car '(1 2 3)) (list 2 3 4)) (cons 2 3))`

(c) `(define a 4)`
`((lambda (x y) (+ a)) 1 2)`

(d) `((lambda (x y z) (y x)) 2 / 2)`

(e) `((lambda (x) (x x)) (lambda (y) 4))`

(f) `(define boom1 (/ 1 0))`

(g) `boom1`

(h) `(define boom2 (lambda () (/ 1 0)))`

(i) `(boom2)`

(j) How can we rewrite `boom2` without using the `lambda` operator?

2. What will Scheme output?

(a) `(if 0 (/ 1 0) 1)`

(b) `(and 1 #f (/ 1 0))`

(c) `(and 1 2 3)`

(d) `(or #f #f 0 #f (/ 1 0))`

(e) `(or #f #f (/ 1 0) 3 4)`

(f) `(and (and) (or))`

3. `let` is a special form in Scheme which allows you to create local bindings. Consider the example

```
(let ((x 1)) (+ x 1))
```

Here, we assign `x` to 1, and then evaluate the expression `(x + 1)` using that binding, returning 2. However, outside of this expression, `x` would not be bound to anything.

Each `let` special form has a corresponding lambda equivalent. The equivalent lambda expression for the above example is

```
((lambda (x) (+ x 1)) 1)
```

The following line of code does not work. Why? Write the lambda equivalent of the `let` expressions.

```
(let ((foo 3)
      (bar (+ foo 2)))
  (+ foo bar))
```

2 Scoping

1. What is the difference between dynamic and lexical scoping?
2. What would this print using lexical scoping? What would it print using dynamic scoping?

```
a = 2
def foo():
    a = 10
    return lambda x: x + a
bar = foo()
bar(10)
```
3. How would you modify an environment diagram to represent dynamic scoping?

3 Code-Writing

1. Implement `waldo`. `waldo` returns `#t` if the symbol `waldo` is in a list. You may assume that the list passed in is well-formed.

```
scm> (waldo '(1 4 waldo))
```

```
#t
```

```
scm> (waldo '())
```

```
#f
```

```
scm> (waldo '(1 4 9))
```

```
#f
```

```
(define (waldo lst)
```

```
)
```

2. **Extra challenge:** Define `waldo` so that it returns the index of the list where the symbol `waldo` was found (if `waldo` is not in the list, return `#f`).

```
scm> (waldo '(1 4 waldo))
```

```
2
```

```
scm> (waldo '())
```

```
#f
```

```
scm> (waldo '(1 4 9))
```

```
#f
```

```
(define (waldo lst)
```

```
)
```

4 Challenge Question

3. **(Optional)** The quicksort sorting algorithm is an efficient and commonly used algorithm to order the elements of a list. We choose one element of the list to be the pivot element and partition the remaining elements into two lists: one of elements less than the pivot and one of elements greater than the pivot. We recursively sort the two lists, which gives us a sorted list of all the elements less than the pivot and all the elements greater than the pivot, which we can then combine with the pivot for a completely sorted list.

Implement `quicksort` in Scheme. Choose the first element of the list as the pivot. You may assume that all elements are distinct. Hint: you may want to use a helper function.

You may additionally want to use the built-in `append` function, which takes in two lists and returns a new list containing the elements of the first list followed by the elements of the second list. You can also use `filter` procedure, which takes in a one-argument function and a list and returns a new list containing only the elements of the original list for which the function returns true, although it is not required.

```
scm> (quicksort (list 5 2 4 3 12 7))
(2 3 4 5 7 12)
```